Lubricant Jet Flow Phenomena in Spur and Helical Gears With Modified Center Distances and/or Addendums—for Out-of-Mesh Conditions

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ABSTRACT

The work reported is an extension from a previous study which was limited to standard centers and tooth proportions only. This paper includes long and short addendums and modified center distances. The analysis develops the equations for the limit values of variables necessary to remove prior severe limitations or constraints necessary to facilitate computer analysis. A new computer program IMPOUT2 has been developed using these newly established "Limit Formulas" to prevent negative impingement on the pinion. The industrial standard nozzle orientation usually found where the offset "S = 0" and inclination angle " β = 0" will often cause the pinion to be deprived of primary impingement which can be an important cause of incipient scoring failure in high-speed drives.

NOMENCLATURE

 $C + \Delta a_p + a_g = operating center distance (in.)$ impingement distance for pinion (see fig. 3) (in.)

impingement distance for gear (see fig. 5) (in.)

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number of teeth in pinion and gear respectively
 N<sub>p</sub>,N<sub>g</sub>
R
                         standard pitch radius of gear
 R_a = R_x \cos \beta
                         perpendicular distance from gear center (in.)
                         base radius of gear (in.)
                         (R_{or}^2 - R_s^2)^{1/2} offset normal (in.)
                         R_0 + \Delta a_q operating outside radius of gear (in.)
 R_r = C_r N_q /
                         running or operating pitch radius
                           of gear (in.)
                         R_{\perp} + S radius to gear offset from gear center (in.)
                         gear radius to coincidence of O.D.'s (in.)
                         offset of jet stream on gear 0.0. (see figs. 1 and 2)
                           (in.)
                         dimensionless offset
 S_1 = S/S_0
S<sub>4</sub>(min)
                         minimum theoretical dimensionless offset when
   = S(min)/S_0
                           d_p(max) = 0 and V_1 = simultaneously (see
                           figs. 11 and 12)
Sn
                         offset of jet to crotch (or coincidence) of O.D.'s (see
                           fig. 1) (in.)
                        offset of jet stream on pinion O.D. (see fig. 4) (in.)
                        oil jet velocity from nozzle exit (in./sec)
                        jet velocity when d_{D} = 0 for given \omega_{D} (in./sec)
   min
                        operating gear addendum (in.)
                        operating pinion addendum (in.)
                        depth of impingement on gear (in.)
                        depth of impingement on pinion (in.)
d (max)
                        maximum theoretical depth on pinion
                        involute function of \phi_{og} (typical) (rad.)
                        gear reduction ratio
                        normal diametral pitch
                        standard pitch radius of pinion
r_a = r_x \cos \beta
                        perpendicular distance for pinion center (in.)
r_h = r \cos \phi_t
                        base radius of pinion (in.)
                        operating outside radius of pinion (in.)
r_{or} = r_0 + \Delta a_p
r_r = \frac{C_r N_p}{(N_p + N_g)}
                        running or operating pitch radius of pinion (in.)
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offset radius from pinion center (in.)
                          pinion radius to coincidence of O.D.'s (in.)
                          generalized time of jet flight and gear rotation (sec)
                          total time of flight to jet impingement (sec)
                          total time of rotation (sec)
                          arbitrary offset distance from S (see fig. 2) (in.)
                          arbitrary inclination angle of jet stream (rad.)
 + \beta_1 = (\beta - \beta_0)/
                          normalized positive inclination angle
   (\beta \max - \beta_p)
 -\beta_1 = (\beta - \overline{\beta}_p)/
                          normalized negative inclination angle
   (\beta_n - \beta \min)
                          maximum inclination angle permitted
                          minimum inclination angle permitted
 Bmin
                          inclination angle when jet passes through pitch point
                             (rad.)
                          inclination angle when jet passes through crotch of
                            0.D.'s and pitch point (S = S_0) (rad.)
 \delta = d P_n/2
                          dimensionless impingement depth, pinion or gear

\Delta a_g = \Delta N_g / g

(2P_n \cos \psi)

                          gear addendum modification (in.)

\begin{array}{c}
\Delta a \\
p \\
= \Delta N_p / (2P_n \cos \psi)
\end{array}

                          pinion addendum modification (in.)
                          tooth addendum modification for \Delta a_{\alpha}
                          tooth addendum modification for \Delta a_n
\Delta P^{D}
                          differential jet pressure at nozzle exit (psi)
                          angular velocity of pinion (rad/sec)
\omega_{_{
m D}}
                          normal pressure angle (rad.)
Φn
^{\varphi}_{\text{og}}
                          pressure angle at O.D. of gear (rad.)
                          pressure angle at lowest impingement point on pinion
φ<sub>D</sub>2
                            (rad.)
                          pressure angle at o.D. of pinion (rad.)
Фор
                          tangential standard pressure angle (rad.)
                          tangential operating pressure angle (rad.)
\Phi_{	t t r}
                         helix angle (deg.)
θgì
                         initial position of gear tooth at beginning of pinion
                            impingement cycle (t = 0) (rad.)
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 θ_{g2} initial position of gear tooth at beginning of gear impingement cycle (rad.) θ_{g3} final position of gear at max. impingement depth $(t_f = t_w)$ (rad.) θ_{p1} initial angular position of pinion tooth at beginning of pinion impingement cycle (t = 0) (rad.) θ_{p2} final position of pinion tooth at maximum impingement depth $(t_s = t_w)$ (rad.) θ_{p3} final position of pinion tooth when just missed by jet stream (t = 0) (rad.) θ_{p4} initial position of pinion tooth at beginning of gear impingement cycle (t = 0) (rad.)

INTRODUCTION

In the gearing industry, gears are lubricated and cooled by various methods. At low to moderate speeds and loads, gears may be partly submerged in the lubricant which provides lubrication and cooling by splash lubrication (ref. 1). With splash lubrication, power loss increases considerably with speed as shown in Ref. 1. This is partially because of churning losses. In Ref. 2 it is shown that gear scoring and surface pitting can occur when the gear teeth are not adequately lubricated and cooled. The results of Ref. 3 for spur gear oil jet lubrication show that as the gear pitch line velocity increases at a constant into-mesh lubrication condition, the limiting tooth load that will cause gear scoring is drastically reduced. This is primarily because the method of lubrication does not provide adequate cooling at the increased pitch line velocity. In a study of high speed heavy duty gears (ref. 4) the authors showed that the oil jet location and amount of oil flow to the gears varies nearly linearly with gear pitch line velocity and also with tooth load. In Ref. 5 the authors showed that with radial jet lubrication the gear tooth temperature at various speed and loads can be considerably reduced by increasing the lubricant jet pressure and flow rate to obtain better cooling. It was shown in Refs. 5 and 6 that the oil jet lubrication is the most effective method when the jet is directed in the radial direction with adequate pressure and flow. Many gears are lubricated by directing the oil jet at the engaging side of the mesh (into mesh lubrication) or at the disengaging sides of the gear mesh (out of mesh lubrication). In Refs. 7 and 8. the authors analyzed oil jet lubrication when the oil jet is directed at the

engaging side of the gear mesh. In Refs. 7 and 8 it was shown that there is an optimum oil jet velocity and oil jet location to obtain the best lubrication and cooling for into-mesh lubrication.

In Ref. 9 the oil jet lubrication for out of mesh lubrication was analyzed and the oil jet impingement depth was determined for standard gearing dimensions. Also in Ref. 9 the oil jet location an direction were limited to a no offset condition (directed at the pitch point only) and in a direction normal to the line of center. This method will give good results for standard gear dimensions with gear ratios close to unity. However, when nonstandard dimension, spread center distance, etc. and large gear ration are used the oil jet direction and location should be changed to provide the optimum oil jet impingement depth and maximum cooling condition.

The objective of the work reported herein is to analyze the out of mesh jet lubrication with most of the simplifying constraints used in reference 9 removed. Since most high performance gears require addendum modifications and in addition sometimes spread centers, the analysis presented herein set out to include these and other related conditions. One practical constraint is added: a nozzle orientation that allows a pinion or gear to be missed provides no primary cooling to the missed member. Such solutions are not permitted in this analysis since they are not of practical value and can mislead an inexperienced gear design engineer.

BRIEF DESCRIPTION OF THE IMPINGEMENT CYCLE

The beginning of the pinion impingement cycle is about to start as the leading edge of the top land of the gear is passed as shown in Fig. 1. Gear tooth rotation continues toward the jet stream until the jet reaches the trailing edge of the gear tooth as shown in Fig. 2. At this position the time t is set at zero (t = 0) and the geometrical position of the gear θ_{gl} is calculated. Also the initial position of the pinion θ_{pl} is calculated at (t = 0). Then the geometry of the lowest impingement point on the pinion is established by setting the time of flight of the jet stream head equal to the time of rotation on the pinion from (t = 0) until impingement on the pinion takes place at θ_{p2} as shown in Fig. 3, ($\theta_{tf} = t_w$). Figure 4 shows the initial position of the jet head ($\theta_{tf} = t_w$). Figure 4 shows the initial position of the jet head ($\theta_{tf} = t_w$) when the impingement flow toward the lowest impingement point on the gear is initiated. Here the initial position of the pinion is θ_{p4} and θ_{g2} for the gear. Again the times of

flight and rotation are equated ($t_f = t_w$). Impingement at the lowest point on the gear (t_g) is shown in fig. 5. The gear position is θ_{g3} at this lowest point of impingement.

Thus the depth of primary impingement on the gear is d_g as shown in the figure. When the jet velocity V_g is reduced below V_j (min) the pinion is missed and the impingement depth on the gear is not increased as expected but reduced.

MODEL CONTROLS AND RESTRAINTS

Development of the mathematical model used in Ref. 1 was restricted to spur gears and the nozzle position was restricted to the arbitrary offset distance S=0 and arbitrary inclination angle $\beta=0$ orientation. The geometric definition of S and β are described below and shown in Fig. 1. The above restrictions have been removed in this mathematical development. Also the origin for the jet stream trajectory is defined as the position where the jet crosses the gear outside diameter (0.0.) as shown in Fig. 1 at A, B, and C. Position A shows the general case where $0 < S < S_0$ and B is a special case where $S=S_0$ and C is the classic case where S=0 pointing at the pitch point and perpendicular to the line of centers.

In this paper the value of the arbitrary offset S where the jet line crosses the gear I.D. is restricted to $S(min) \le S \le S_0$ where

$$S_0 = \frac{(a_{gr}^m_q - a_{pr})}{m_q + 1} + \frac{a_{gr}^2 - a_{pr}^2}{2r_r(m_q + 1)}$$
(1)

as shown in Fig. 1 (see Nomenclature for variable definitions not described in text). Thus the operating (or running) offset S_0 to the crotch or common intersection of the outside diameters is the maximum value allowed for the offset S to remain within the geometric definitions described in this paper. Further when the addendum modification Δa_{pr} and Δa_{gr} are unequal and extreme enough to cause S_0 to be negative then $S_0 \leq S \leq 0$. Also when $\Delta a_{pr} = \Delta a_{qr} = \Delta a_{qr} = 0$ with standard centers, S_0 reduces to

$$S_0(Std) = (1/(P_n \cos \psi))((N_g/N_p) - 1)/((N_g/N_p) + 1) = a(m_g - 1)/(m_g + 1)$$

Also the inclination angle ß is confined to point at the line of centers between the confines of the outside diameters of the pinion and gear respectively as shown in Fig. 1.

The inclination angle β is considered positive when slanted from right to left through the point of origin A, B, or C as shown in Fig. 1. At $\beta=0$ the jet is pointed perpendicular to the line of centers, and when β is negative it is slanted from left to right through the point of origin on the 0.D. of the gear, not shown in Fig. 1. It is not usually considered wise to use negative β angles with near standard proportion gears lest we starve the gear of adequate coolant.

The mathematical definition of the arbitrary inclination angle B is:

$$\beta = \tan^{-1} (x/R_1) \tag{2}$$

where:

$$R_1 = (R_{or}^2 - R_s^2)^{1/2}$$
 and

x = an arbitrary offset distance from "S" position to where the jet stream crosses the common line of centers.

$$R_{or} = R_{o} + \Delta a_{g} = \text{Operating outside radius}$$

$$R_{0} = N_{g}/(2P_{n}cos\psi) + 1/P_{n} = \text{Std. 0.D., gear}$$

$$R_{s} = R_{r} + S = \text{Radius to offset from gear center}$$

$$R_{r} = C_{r}N_{g}/(N_{g} + N_{p}) = \text{Operating pitch radius, gear}$$

$$\Delta a_{g} = \Delta N_{p}/(2P_{n}cos \psi) = \text{gear addendum modification}$$
 When β is given then,

$$x = R_1 \tan \beta$$
, where β is arbitrary

Thus to remain within the confines established for $~\beta,~\beta_{max},~and~\beta_{min}$ are defined as:

$$\beta_{\text{max}} = \tan^{-1}[(S + a_{pr})/R_1] \text{ and}$$

$$\beta_{\text{min}} = \tan^{-1}[(S - a_{gr})/R_1]$$

Also, for any given offset "S" the angle β_p to the pitch point is (used as a normalizer);

$$\beta_{\rm p} = \tan^{-1}(S/R_1) \tag{3}$$

and further if $S = S_0$ then the angle to the pitch point is

$$\beta_{\rm DD} = \tan^{-1}(S_0/R_1)$$

since β can be arbitrarily selected, it is necessary to provide the user with a normalized (dimensionless) input value for β that won't be out of bounds of the solvable geometry. This is done here using the β_1 input parameter where $-1 \leq \beta_1 \leq 1$ and is defined as; when β_1 is positive (+):

$$\beta_1 = \frac{\beta - \beta_p}{\beta_{\text{max}} - \beta_p}, + \beta = \beta_1(\beta_{\text{max}} - \beta_p) + \beta_p$$
 (4)

and when β_1 is negative (-):

$$\beta_1 = \frac{\beta - \beta_p}{\beta_p - \beta_{min}}, + \beta = \beta_p - \beta_1(\beta_{min} - \beta_p)$$
 (5)

so that when;

 $\beta_1 = 0 : \beta = \beta_D$ (pointing at pitch point)

 $\beta_1 = 1 : \beta = \beta_{max}$ (pointing at 0.D. pin.)

 $\beta_1 = -1$: $\beta = \beta_{min}$ (pointing at 0.D. gr.)

Further if the user desires to know the value of β_1 that will make $\beta=0$, he calculates β_{10} from:

$$\beta_{10} = \frac{\beta_p}{\beta_{min} - \beta_p}$$
 if β_{10} is negative as is usual

Similarly, when S is normalized we get:

$$S_1 = S/S_0 \tag{6}$$

where the value of S_1 is confined to $S_{1(min)} \leq S_1 \leq 1$.

Thus the use of the computer program IMPOUT2 can be entered using S_{ij} and B_{ij} without knowing S or B with some relative feel for where the jet nozzle is pointing.

A further constraint of paramount importance is $S_{1(min)}$ so defined, given β_1 or β and Δa_p and Δa_g , so that $d_{p(max)} = 0$ thus making the pinion 0.D. barely reachable when the jet velocity V_j approaches infinity. This further confines S_1 so that $S_{1(min)} < S_1 \le 1$ to maintain impingement at least on the top land of the pinion, where S_1 is found by iterating:

$$abs \left[r_{or}^{2} - r_{a}^{2} + L_{p}(min)^{2} \right] \le 10^{-3}$$
 (7)

as a function of S(min) with given β and $\Delta a_{p,g}$ until the inequality is satisfied when the above restraints on S_1 , B_1 , Δa_p , and Δa_g are given, the user of the program IMPOUT2 is assured of impingement on the pinion. $d_n(max)$ is defined later in this paper.

Once S(min) is found from Eq. (7), $S_{i(min)}$ can be calculated from: $S_{i(min)} = S(min)/S_{o}$ (8)

DEVELOPMENT OF THE GEOMETRIC MODEL FOR THE PINION

The problem to be solved here depends on what is given. If the jet velocity is given then we solve explicitly for the impingement depth d_p so that subsequently this depth can be used to determine the cooling effect on the pinion and gear respectively. On the other hand, if the desired depth of impingement is given, and $d_p < d_p(\max)$, then the desired jet velocity "V₁" can be calculated explicitly from the equation:

$$V_{jp} = \left(\left(\left(R_{or}^2 - R_s^2 \right)^{1/2} sec \beta - \rho_x \sin \beta - L_p \right) \omega_p \right) / (\theta_{p2} - \theta_{p1})$$
 (9)

where

angular velocity (rad/sec) helix angle

```
number teeth on pinion
                                 number of teeth on gear wheel
 \Delta a_p = \Delta N_p /
                                 pinion addendum modification
   (2P<sub>n</sub>cosψ)
 r_{y} = r_{r} - S + x
                                 radius to jet stream intersection on line of centers
                                    from pinion center (see fig. 2)
                                 pinion operating pitch radius (in.)
 r_r = C_r N_n /
 C_r = C + \Delta a_p + \Delta a_g
                                 operating center distance (in.)
                                 impingement distance (in.), (see fig. 3)
 r_{or} = r_{o} + \Delta a_{p}
                                 operating outside radius of pinion (in.)
 r_0 = N_p/(2P_n \cos \psi)
                                 outside radius of pinion (see fig. 1)
 r_a = r_y \cos \beta
                                 perpendicular distance from pinion center (see
                                   fig. 2)
                                 impingement depth from pinion O.D. (in.) (see fig. 3)
                                 jet head position t = 0 (see fig. 2)
                                gear ratio (see fig. 2)
                                operating pressure angle (see fig. 5)
   (N_1\cos\phi_{\dagger}/(N_1 + (2p_n\DeltaQ_1)))
                                transverse pressure angle
  (tan\phi_n/cos\psi) = cos^{-1}(R_h/R)
                                normal pressure angle at pitch radius
inv_{tr} = tan_{tr}
                                radians (see fig. 4)
\theta_{gl} = \cos^{-1}(R_s/R_{or}) - \ln \phi_{og} + \ln \phi_{tr} (see fig. 1)
\phi_{0g} = \cos^{-1}
                                pressure angle at gear O.D.
inv_{og} = tan_{og}
                                radians (see fig. 2)
\theta_{p2} = tan^{-1}
                                radians
  (L_p/r_a) + 1nv\phi_{p2}
```

As will be seen by reviewing the input parameters, a substantial amount of calculation is required before Eq. (7) for V_{jp} can be solved. Thus a computer program is required to do the job reliably, such as the program IMPOUT2 as mentioned above.

Generally solving for the required velocity to obtain a desired depth "dp" on out-of-mesh cooling would be unusual mainly because of the limit imposed by "dp(max)" which is the limiting depth of impingement when $V_j \rightarrow \infty \quad \text{so that } 0 < d_p < d_p(\text{max}). \quad d_p(\text{max}) \quad \text{is calculated from:}$

$$d_p(max) = r_{or} - \left(r_a^2 + L_p(min)^2\right)^{1/2}$$
 (10)

where:

$$L_p(min) = r_a \tan (\theta_{pl} - inv \phi_{p2})$$

Note that $\phi_{p2} = f_n(L_p)$ and $L_p = f_n(S + \beta)$ as $V_j \rightarrow \infty$

In real geared systems the jet velocity " V_g " is already specified by the system lubricant pressure so that we solve for d_p within the range $0 < d_p < d_p (max)$ which is usually quite narrow. It is necessary when " V_g " is given to solve for d_p implicitly using an iterative technique. This can be accomplished by solving for the impingement distance L_p (see fig. 3) implicitly using the equation:

$$L_{p} = \frac{\left(R_{or}^{2} - R_{s}^{2}\right)^{1/2}}{\cos \beta} - \frac{V_{1}(\theta_{p2} - \theta_{p1})}{\omega_{p}} - r_{x}\sin \beta$$

with V_j given and noting that $\theta_{p2} = f_n(L_p)$.

Then the depth of impingement on the pinion is:

$$d_p = r_{or} - \left(r_a^2 + L_p^2\right)^{1/2}$$
 (12)

where: $0 < d_p < d_p \text{(max)}$ and a negative d_p means that the jet missed the pinion.

Missing the pinion (or neg. d_p) can be avoided by proper placement of the nozzle offset "S" where S(min) < S < S₀ as established above and/or V_1 (min) < V_1 < ∞ where; (see fig. 6).

$$V_{j}(m1n)_{p} = \frac{((R_{or}^{2} - R_{s}^{2})^{1/2} - (r_{or}^{2} - r_{a}^{2})^{1/2} - r_{x}s1n \beta)\omega_{p}}{(\theta_{p3} - \theta_{p1})}$$
(13)

where

$$\theta_{p3} = \cos^{-1}(r_a/r_{or}) + inv\phi_{op}$$
 (radians)
 $\theta_{op} = \cos^{-1}(r_b/r_{or})$ and
 $inv\phi_{op} = tan \phi_{op} - \phi_{op}$ (radians)

Equation 13 provides the minimum velocity to reach the top land of the pinion for the selected offset S when S(min) < S and $d_p = 0$, assuming that S_0 is positive.

DEVELOPMENT OF THE GEOMETRIC MODEL FOR THE GEAR

In the case of the gear meshing with the pinion, the jet velocity of the gear is common with that for the pinion; so that even if the velocity V_{jp} is found explicitly to provide a desired or specified depth of impingement on the pinion "dp", the jet velocity for the gear is always provided by $V_{jp} = V_{gp} = V_{j}$ so that the impingement depth for the gear is always found for the implicit solution for L_{p} from the equation:

$$L_{g} = \frac{(r_{or}^{2} - r_{sp}^{2})^{1/2}}{\cos \beta} + r_{x} \sin \beta - \frac{V_{1}(\theta_{q3} - \theta_{q2})}{\omega_{q}}$$
 (14)

where we note that

Then the impingement depth on the gear is calculated from:

$$d_g = R_{or} - \left(R_a^2 + L_g^2\right)^{1/2}$$
COMPUTERIZED PARAMETRIC STUDY

A rather intricate computer program has been developed which should be useful to the design engineer as well as the researcher performing parametric studies. This program "IMPOUT 2" was used in the study for this section of the paper.

The out-of-mesh nozzle orientation imposes severe impingement depth problems especially when the gear ratio is larger than one-to-one. This is demonstrated in Fig. 7 where it can be seen that when the gear ratio "mg" is equal to one (1.0) the depth of jet oil impingement is equal on pinion and gear for a perpendicular jet pointed at the pitch point. However, when man is larger than unity, the impingement depth on the pinion is very dependent on the offset "S". This is shown in Fig. 7 using the dimensionless offset S_4 . As can be seen when $S_1 = 1.0$, the position at the intersection of the pinion and gear 0.D.'s the jet is pointed at the pitch point β_1 = 0. Both pinion and gear have near equal impingement depth. But as the offset S_1 is lowered or the gear ratio is increased, the impingement on the pinion rapidly disappears. In the figures at $S_i = 0.96$, the depth disappears at $m_g = 6.0$ and at $S_1 = 0.863$ it disappears at 2.5, and at $S_1 = 0$ it disappears at 1.2. Obviously, when $S_1 = 0$, the pinion receives jet impingement only when m_{α} 1.2. This illustrates the idea that for a given pinion/gear tooth combination we need to know $S_1(\min)$ where no impingement is possible even when the jet velocity V_j approaches infinity $(V_j \rightarrow \infty)$. This then allows solutions for d_p and V_{1p} when $S_1(min) < S < 1.0$. The gear depths $d_{\mathbf{q}}$ area also shown for tooth with a working depth of 0.25 in. and therefore primary impingement can only reach about 1/10th the working depth as shown. Figure 8 shows the effect of the inclination angle $\,\beta_4\,\,$ on pinion impingement depth d_{p} . As expected when the jet pressure is increased so is the impingement depth and as the $\, \beta_{1} \,$ ratio is decreased the depth is increased up to the maximum depth $d_D^{(max)}$ as a function of $S_1^{(max)}$ and $B_1^{(max)}$ per Eq. (10).

Figure 9 shows the effect of offset $\,S_1^{}$ on impingement depth $\,d_p^{}$ and $\,d_g^{}$ on a mesh with long and short addendums and a spread center distance

to accommodate a large gear ratio on a fixed or given center distance. The mesh has been somewhat overcompensated so that S_0 is negative which is rare and reverses the situation such that the gear now is the member that can be easily starved if the jet nozzle is not placed properly. Here, as can be seen, the depth d_g improves as S_1 is increased above $S_1 = 0.6667$ and when optimized by one of the three methods available in IMPOUT2 will still provide an equal impingement depth for both the pinion and gear at dimensionless depth of about $\delta \cong 0.1$, where $\delta = d/\text{whole depth}$. Also usually the program option 3 has a large value than option 2 which is also reversed relative to standard mesh conditions.

Figure 10 shows the results of setting $S_1=0$ and $B_1=0$ and adjusting the pinion and gear addendums to realize the balance of depths of impingement desired. Here as is seen in Fig. 10, as Δa_p is reduced ΔC is reduced and at $\Delta a_p=0.0662$ an equal (or optimum) impingement depth is reached on the pinion and gear. The connected circles at ΔA depict the depths when $\Delta a_p=0.10$ and $\Delta a_q=-0.0375$. Obviously we must optimize using ΔA and ΔA as discussed in Fig. 9. The connected circles at ΔA depicts the depths when ΔA as discussed in Fig. 9. The connected circles at ΔA depicts the depths when ΔA and ΔA are closer together than in "A". Further, when ΔA is further reduced to ΔA and ΔA are closer together than in "B" the depths get much closer together and at ΔA and ΔA are equal.

Figure 11 shows the effect of β_1 on $S_1(min)$. The 21/35 tooth combination was used as the example here. This figure shows that if β is slanted backwards in the negative direction, that S_1 can be made smaller before the pinion is starved. Also if the offset S_1 is set at 1.0 it is nearly impossible to starve the pinion at any reasonable inclination angle β , or β_1 ratio, even when the pressure is modest.

The last Fig. 12 shows the effect of the dimensionless offset S_1 on the minimum velocity or its cause, jet nozzle pressure at the nozzle exit $(V_j(\min) = \text{velocity needed to reach pinion 0.0.})$. As is seen in the figure, $S_j(\min)$ establishes the asymptote where $V_j(\min)$ approaches infinity. This makes it clear that we cannot set S_j below $S_j(\min)$ and expect to obtain primary impingement on the pinion top land or profile at any jet pressure.

DISCUSSION

Figures 11 and 12 show the most important results of this study, in that they point out the importance of careful placement of the nozzle in both position and pointing direction, especially at higher gear ratios considered in Fig. 7. Also for out-of-mesh nozzle orientation, increasing the oil jet presure and velocity to high levels may not always improve the primary impingement depth appreciably as shown in Figs. 9, 10, and 12, and in practical fact may sometimes cause flooding in the gear case or housing. Further, if the inclination angle ß is adjusted to an extreme, per Fig. 8, to improve the impingement depth on the pinion, then the gear depth is diminished usually unacceptably.

Even when the position is fixed in the historically standard orientation position which will not allow primary impingement on the pinion for even modest gear ratios (at any jet pressure), the pinion and gear addendums can be adjusted per Fig. 10 to provide adequate impingement on both mesh members. This has been done in the past to control incipient scuffing or scoring, often without the designer realizing he was also controlling the impingement and cooling phenomena favorably.

SUMMARY OF RESULTS

An analysis was developed for the lubricant jet flow in the out of mesh condition. The analysis provides for the inclusion of modified center distances and modified addendums. The equations are developed for the limit values of variables necessary to remove the severe limitations or constraints necessary to facilitate computer analysis. A computer program was developed using these "Limit Formulas" to prevent negative impingement (missing) on the pinion. The following results were obtained:

- 1. The industrial standard nozzle orientation usually found where the offset S=0 and inclination angle $\beta=0$ will often cause the pinion to be deprived of primary impingement which can be an important cause of incipient gearing failure in high-speed drives.
- 2. For ratios larger than 1:1, the oil jet will only impinge on the gear teeth unless a minimum calculated jet velocity is provided to lubricate the pinion teeth.
- 3. When a minimum oil jet velocity is provided, the oil jet offset must be equal to or greater than a minimum calculated offset to assure impingement on the pinion.
- 4. As the oil jet velocity is increased above the calculated minimum value, the impingement depth will increase but at a decreasing rate. The maximum impingement depth will generally not exceed 10 percent of the tooth profile depth.

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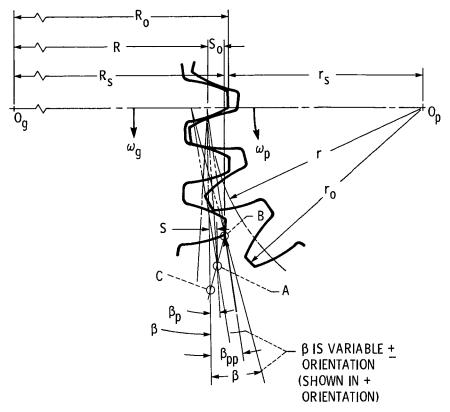


Figure 1. – Jet coordinate origins for impingement on pinion. A = general case where $0 < S < S_0$; B = special case where $S = S_0$; C = classic case where $S = 0^0$.

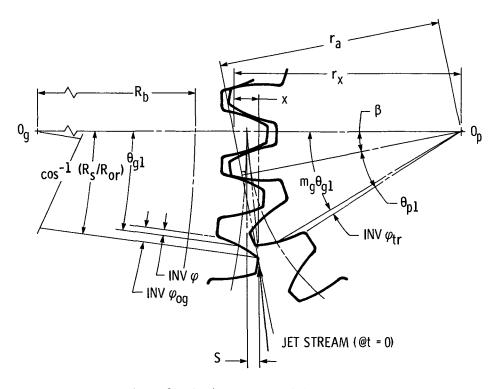


Figure 2. - Impingement on pinion ($@t \approx 0$).

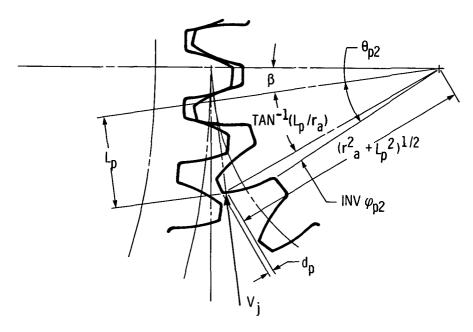


Figure 3. – Impingement on pinion (@ $t_f = t_\omega$).

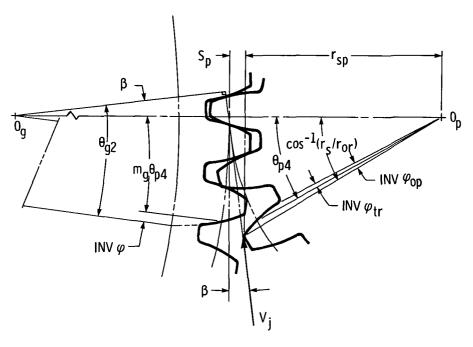


Figure 4. - Impingement on gear (@t = 0).

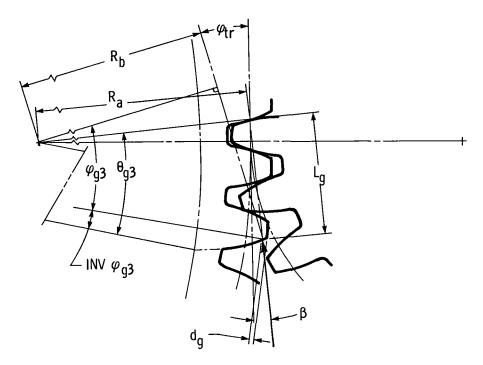


Figure 5. – Impingement on gear (@ t_f = t_ω).

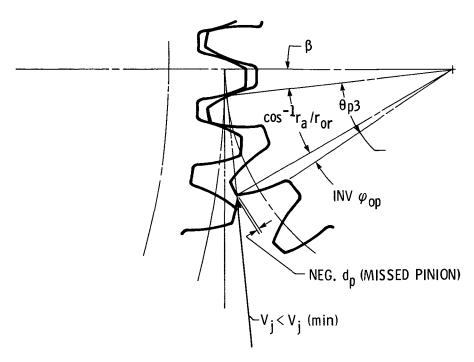


Figure 6. – Missing the pinion when $\textbf{V}_{j}\!<\!\textbf{V}_{j}$ (min).

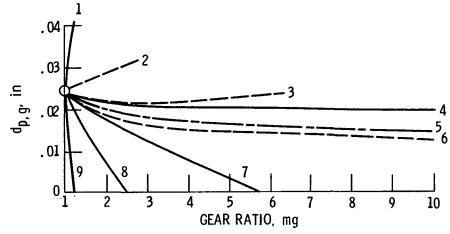


Figure 7. – Effect of gear ratio on impingement depth, β_i = 0. $\Delta\,P$ = 138 psi, n = 5000 rpm, N_p = 28.

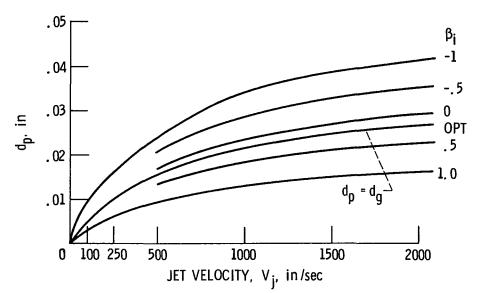
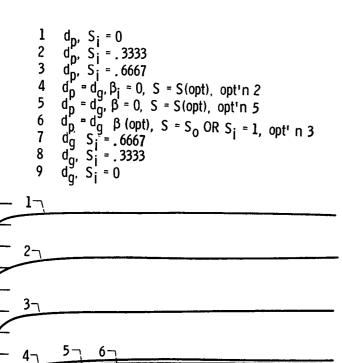


Figure 8. - Effect of β_i on impingement depth, S_i = 1.0, 21/35 combination.



. 10

. 09

.08

. 07

.06

. 05

.03

.01

0

50

d_{p, g}, in

Figure 9. - Effect of offset S_i on impingement depth. 12/43 comb., β_i = 0, Δa_g = -.0375. Δc = .0625, Δa_p = .1, DP = 8, φ = 200.

300

JET PRESSURE, psi

400

500

600

700

97

 d_p , $\Delta a_p = .10$, $\Delta a_g = -.0375$, $\Delta c = .0625$ d_p , $\Delta a_p = .084375$, $\Delta a_g = -.0375$, $\Delta c = .046875$ d_g , $\Delta a_p = .06875$, $\Delta a_n = -.0375$ $d_p = d_g$, $\Delta a_p = -\Delta a_g = .0662$, OPTIMIZED d_g , $\Delta a_p = .084375$, $\Delta a_g = -.0375$ d_p , $\Delta a_p = .06875$, $\Delta a_g = -.0375$, $\Delta c = .03125$ d_g , $\Delta a_p = .10$, $\Delta a_g = -.0375$

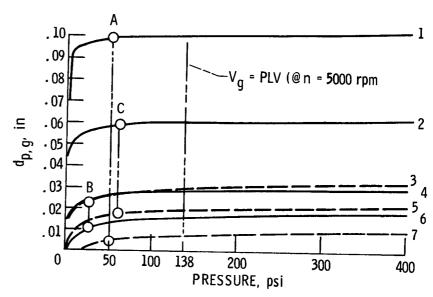


Figure 10. - Effect of addendum modification and spread centers. S_i = 0, β_i = 0, for 12/43 tooth combination.

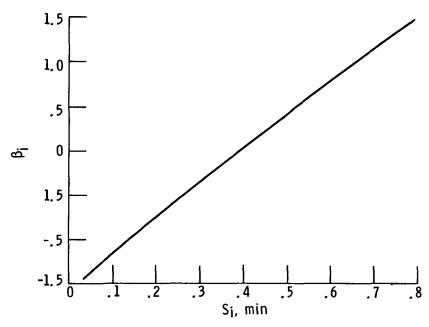


Figure 11. – Effect of β_i on S_i (min), 21/35 combination, φ = 20, P_d = 8.

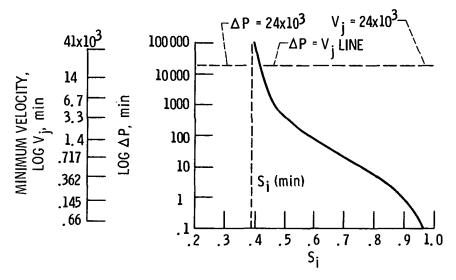


Figure 12. - Minimum differential oil pressure " ΔP (min)" versus dimensionless offset " S_i ", 21/35 combination, 8 DP, 200 PA, β_i = 0, V_j = 156 $\sqrt{\Delta P}$, 5000 rpm.

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